

# Electrostatics of Granular Flow in Pneumatic Systems

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STEP 1 (Static-Tribo-Electricity of Powder) 2014/12/19-12/21  
Soka University, Hachioji, Tokyo, Japan

发展能源技术 共同改变世界

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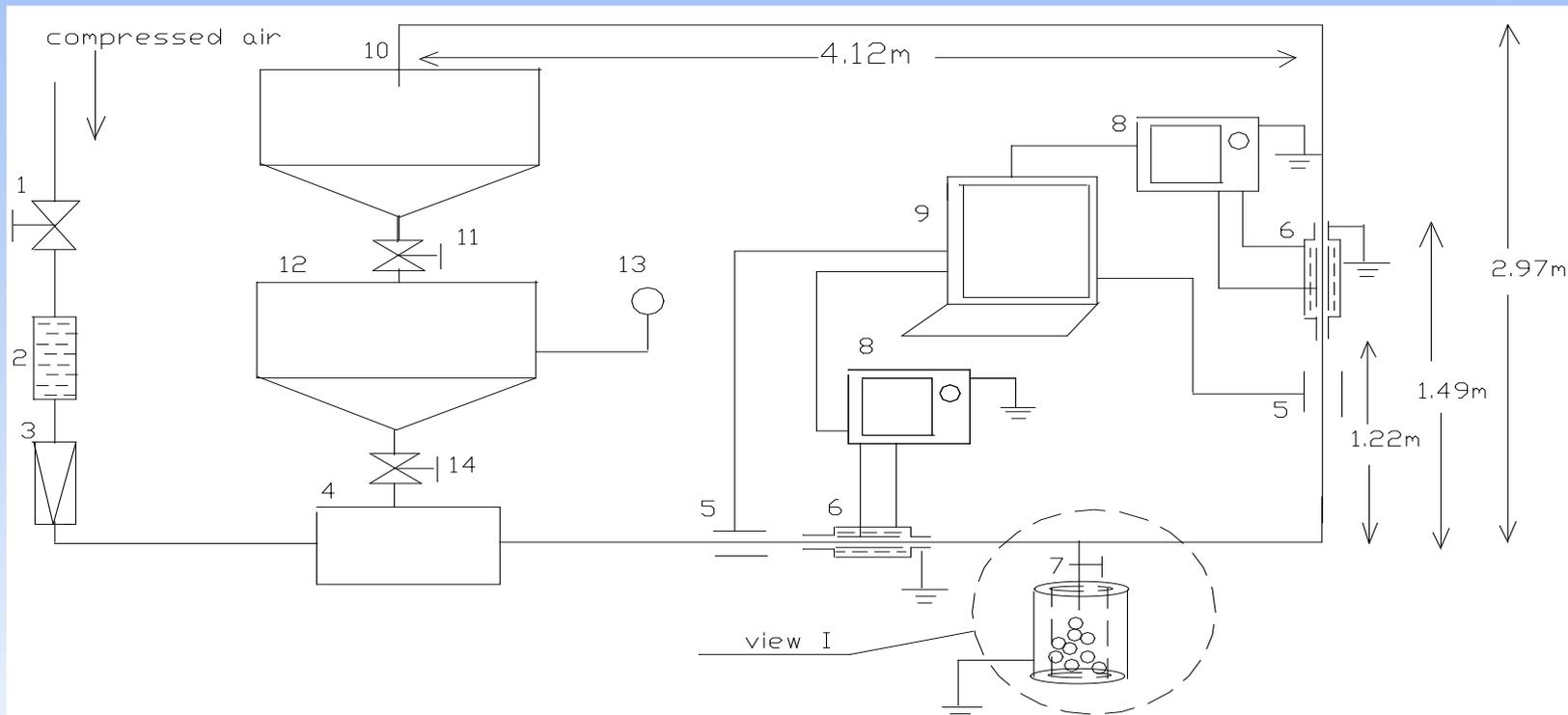


In a polishing workshop powder induced a extremely large accident (96 person die).

Possible reason: particle-particle/particle-wall interaction causes electrostatic charge and charges accumulate, which grows more and more to become explosion source.

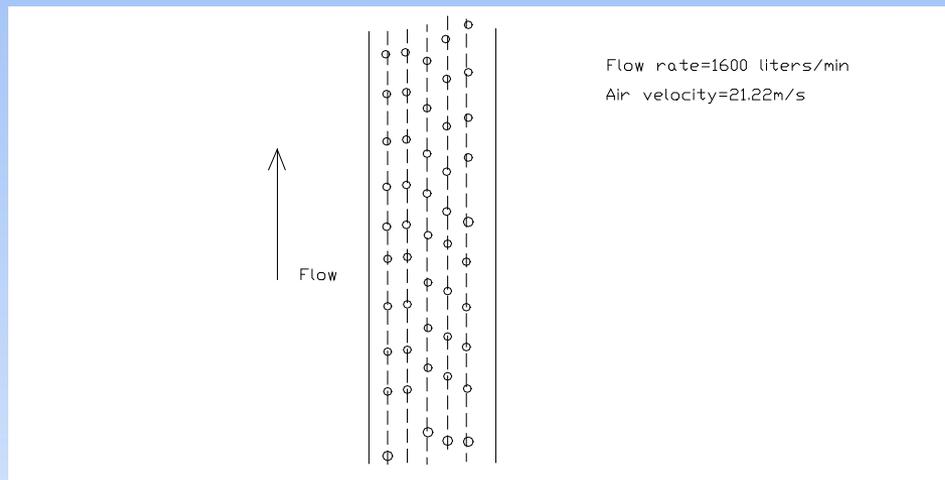


# Experiment setup

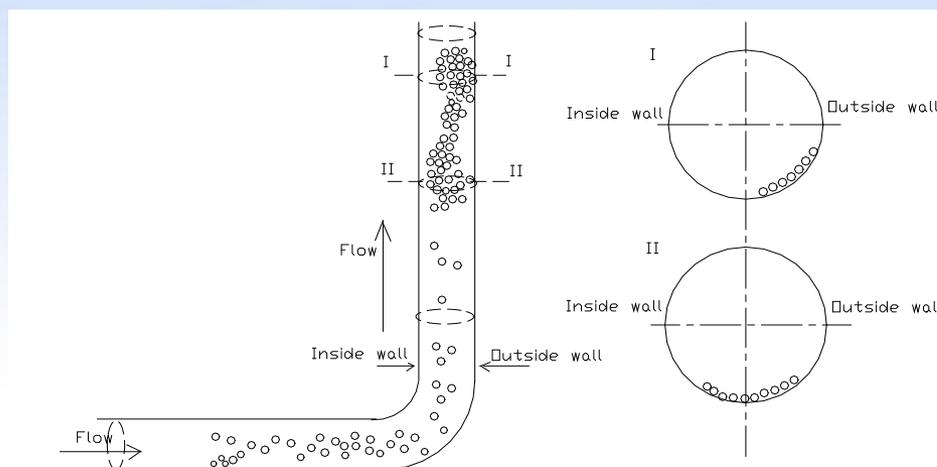


Particles conveying style	Cycle	Particle diameter:	2.8 mm
Particle material:	Polypropylene(PP)	Particle density:	1123 kg/m <sup>3</sup>
Pipe material:	Polyvinyl Chloride (PVC)	Pipe diameter(inner):	40.0 mm
Pipe thickness:	5.0 mm	Relative humidity:	5%
Air flow rate:	860~1600 liters/min	Air superficial velocity:	11.4~21.2 m/s
Temperature:	28~30 ° C		

# Disperse flow -1600 L/min pattern observed in the vertical pipe



**Initial condition**

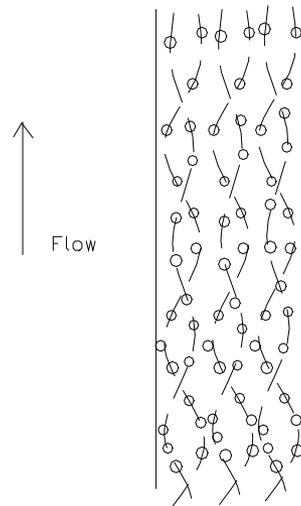


**Two hours later**

The clusters were located fairly high up in the pipe and traveled along a curved path by the pipe wall. These clusters appeared and disappeared intermittently in an unpredictable manner.

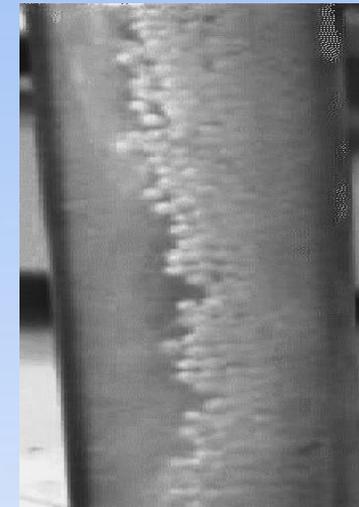
# Half-ring flow – 1100L/min

- vertical granular pattern

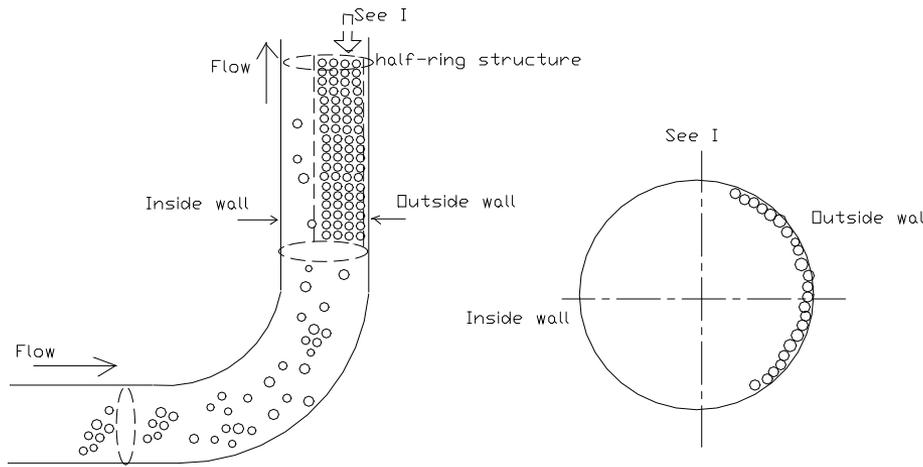


Flow rate=1000-1200 liters/min  
Air velocity=13.263~15.915 m/s

**Initial condition**

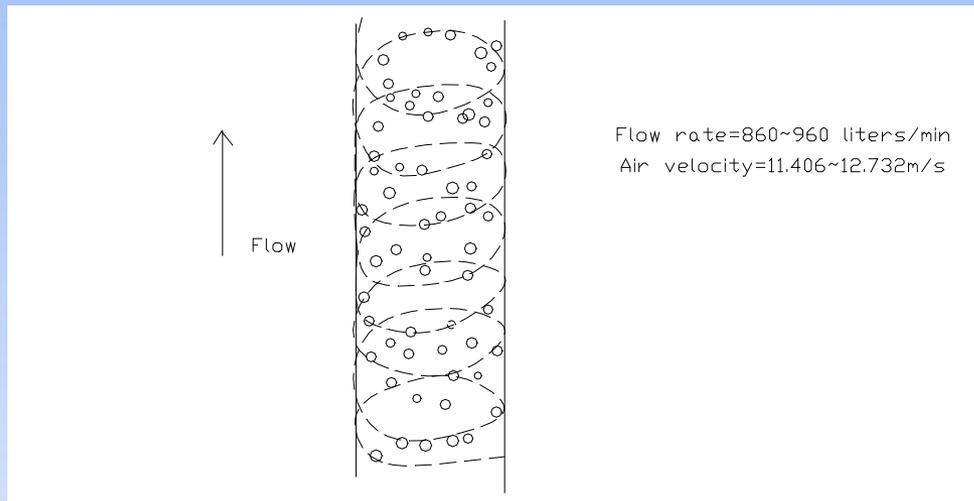


Particles were observed to cluster on the side of the vertical pipe wall distant from the position of the lower horizontal pipe to form a half-annular ring structure

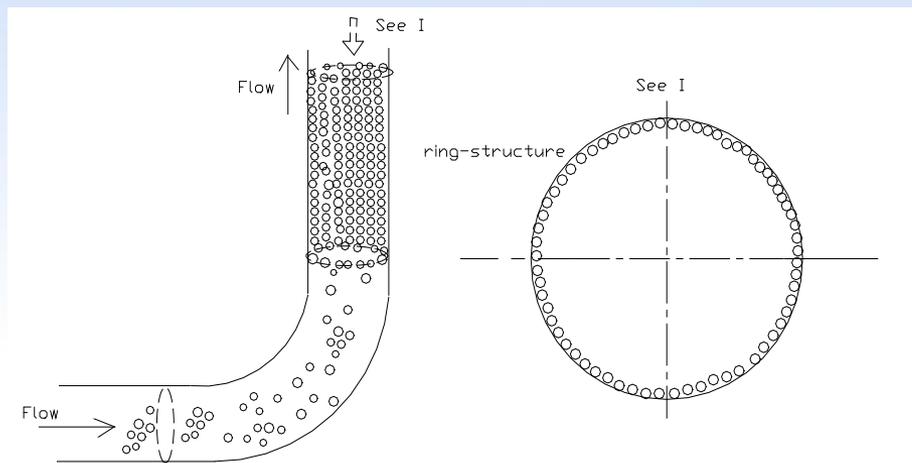
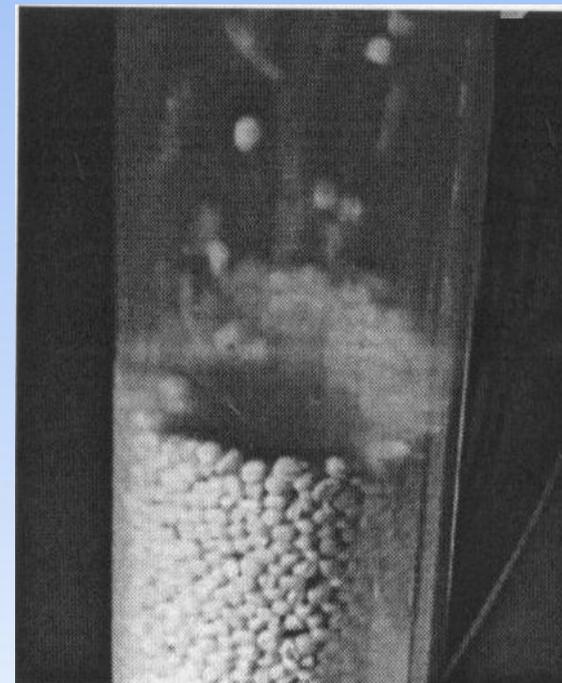


**Half hour later**

# Ring flow – 960 L/min vertical granular pattern

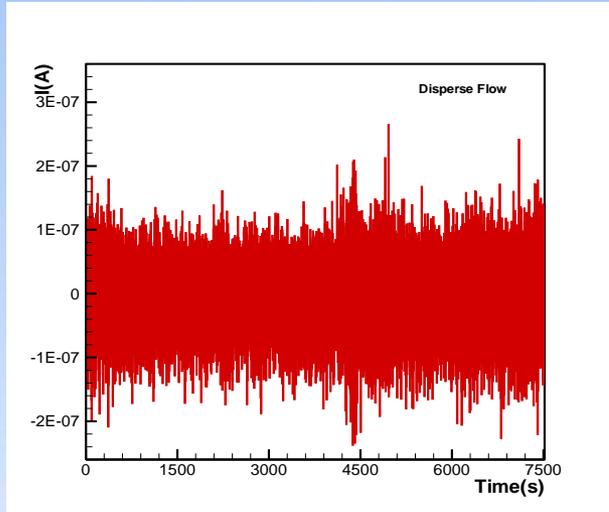


**Initial condition**

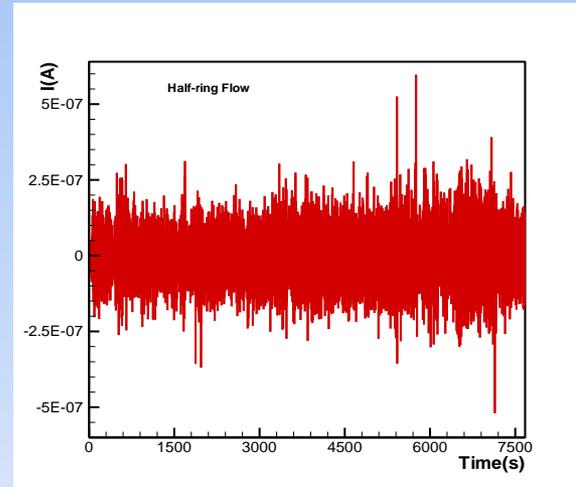


**Fifteen minutes later**

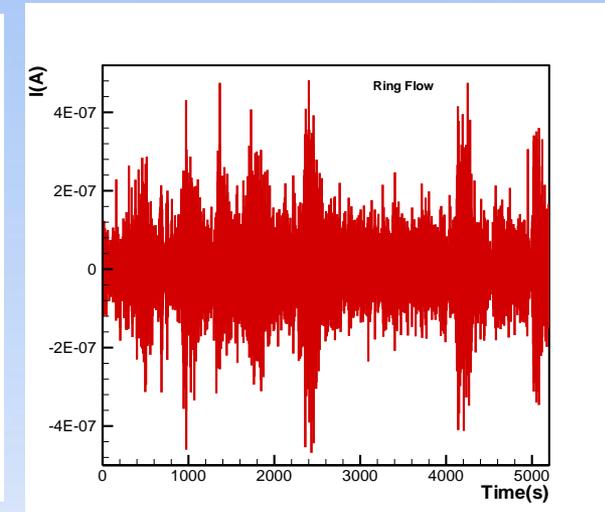
Particles were observed to travel in a spiral fashion up the vertical pipe along the pipe wall. This resulted in a ring or annulus structure with high particle concentrations adjacent to the wall and a relatively empty core region



**Disperse flow**



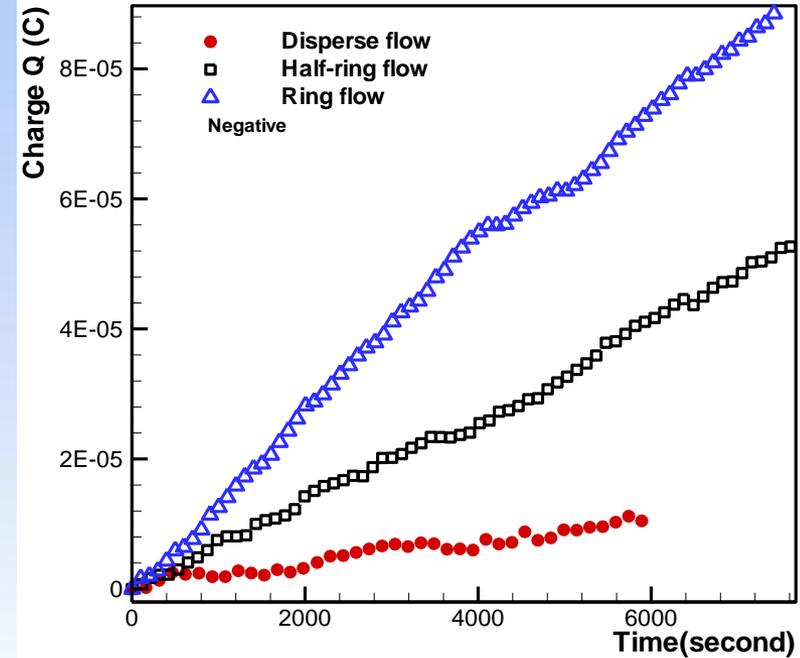
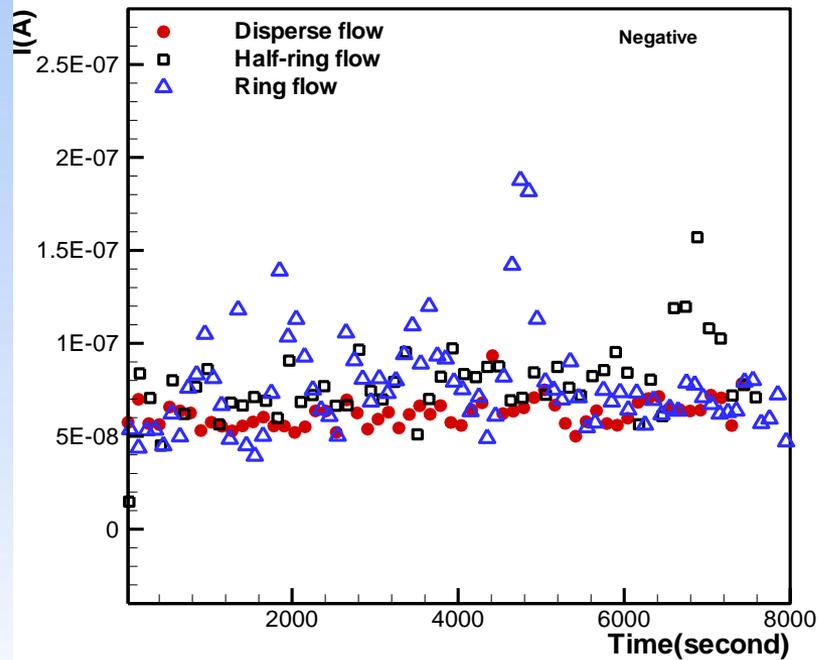
**Half-ring flow**



**Ring flow**

Induced current acquired at the vertical pipe:

- (left) disperse flow (air flow rate 1600 L/min, solids feed rate 35.3 ( 3.2 kg/m<sup>2</sup> s);
- (middle) half-ring flow (air flow rate 1000 L/min, solids feed rate 13.8 ( 2.4 kg/m<sup>2</sup> s);
- (right) ring flow (air flow rate 80 L/min, solids feed rate 8.1( 1.6 kg/m<sup>2</sup> s).



Left: Comparison of the current value (negative) for the three flows.  
Right: Comparison of the charge accumulation for the three flows.

$$e = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r_x^2} \quad (\text{Halliday et al. 1997})$$

$\epsilon_0$ : permittivity constant (in vacuum  $8.85 \times 10^{-12} \text{ C}^2 / \text{N}\cdot\text{m}^2$ )

$r_x$ : the distance from the point charge

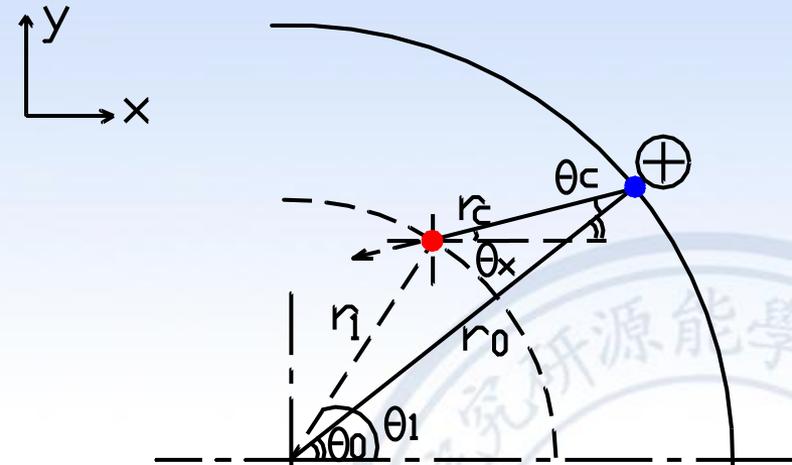
$q$ : the point charge

$$e_x = e \cdot \cos\theta_x = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r_x^2} \cdot \cos\theta_x$$

$$e_y = e \cdot \sin\theta_x = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r_x^2} \cdot \sin\theta_x$$

$$r_x^2 = r_1^2 + r_0^2 - 2 \cdot r_1 \cdot r_0 \cdot \cos(\theta_0 - \theta_1)$$

$$\frac{r_x}{\sin|\theta_0 - \theta_1|} = \frac{r_1}{\sin\theta_{xx}}$$

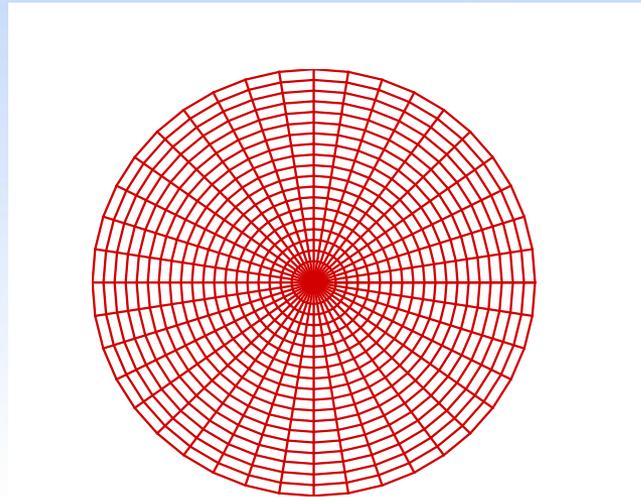


Halliday, D., et al. 1997.

Fundamentals of Physics Extended. 5th ed., P558.

In a two-dimension field, the electrostatic field generated by a point charge  $q$  at the point  $(i, j)$  can be calculated:

$$e_{x(i,j)} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2_{x(i,j)}} \cdot \cos\theta_{x(i,j)} \quad e_{y(i,j)} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2_{x(i,j)}} \cdot \sin\theta_{x(i,j)}$$

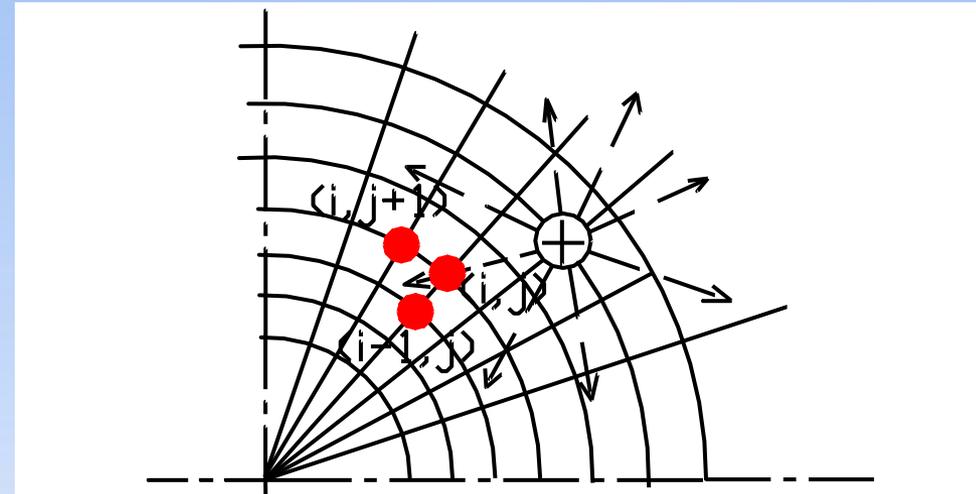


simulation grid (20 × 40)



$$e_{x(l,k,i,j)} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_{(l,k)}}{r_{x(l,k,i,j)}^2} \cdot \cos\theta_{x(l,k,i,j)}$$

$$e_{y(l,k,i,j)} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_{(l,k)}}{r_{x(l,k,i,j)}^2} \cdot \sin\theta_{x(l,k,i,j)}$$

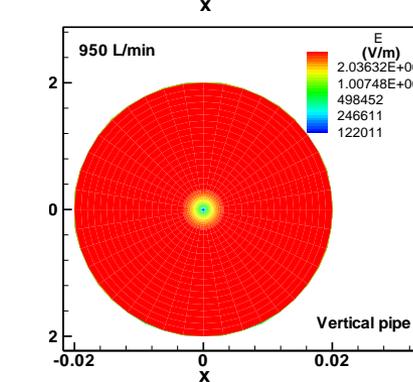
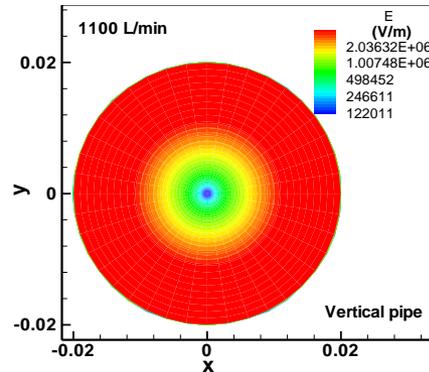
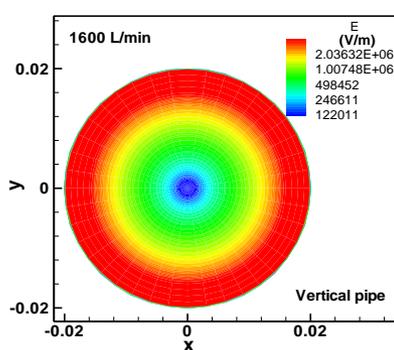
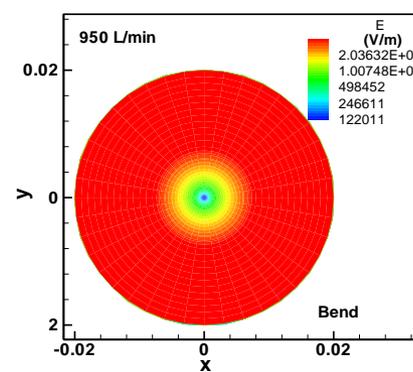
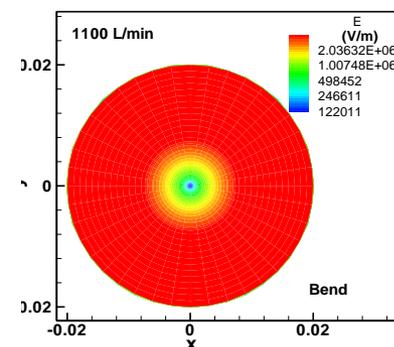
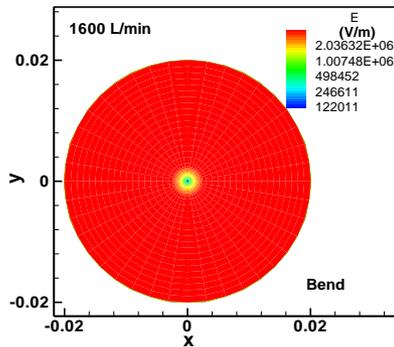
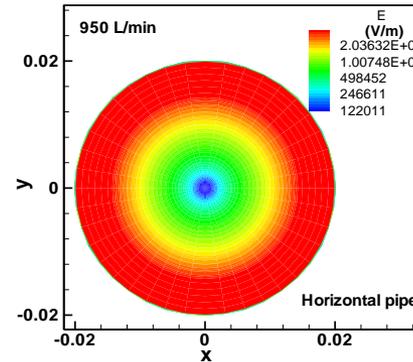
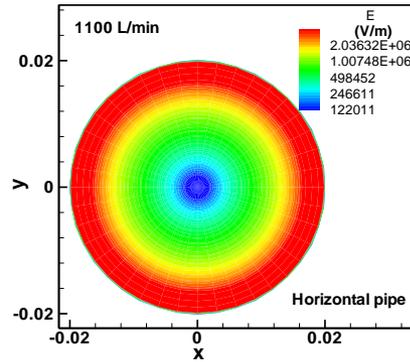
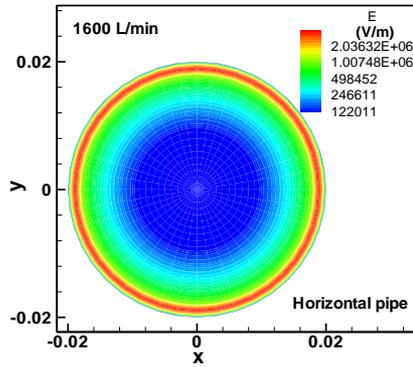


$$E_{x(i,j)} = \sum_{l=1}^m \sum_{k=1}^n \sum_{i=1}^m \sum_{j=1}^n e_{x(l,k,i,j)} = \sum_{l=1}^m \sum_{k=1}^n \sum_{i=1}^m \sum_{j=1}^n \frac{1}{4\pi\epsilon_0} \cdot \frac{q_{(l,k)}}{r_{x(l,k,i,j)}^2} \cdot \cos\theta_{x(l,k,i,j)}$$

$$E_{y(i,j)} = \sum_{l=1}^m \sum_{k=1}^n \sum_{i=1}^m \sum_{j=1}^n e_{y(l,k,i,j)} = \sum_{l=1}^m \sum_{k=1}^n \sum_{i=1}^m \sum_{j=1}^n \frac{1}{4\pi\epsilon_0} \cdot \frac{q_{(l,k)}}{r_{x(l,k,i,j)}^2} \cdot \sin\theta_{x(l,k,i,j)}$$

$$E_{(i,j)} = \sqrt{E_{x(i,j)}^2 + E_{y(i,j)}^2}$$





Horizontal

Bend

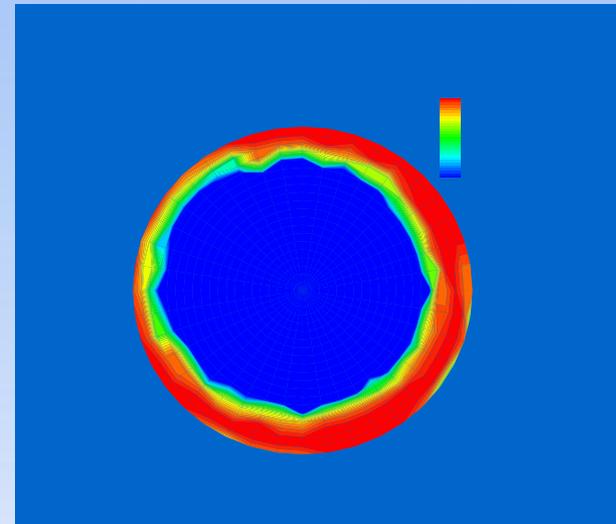
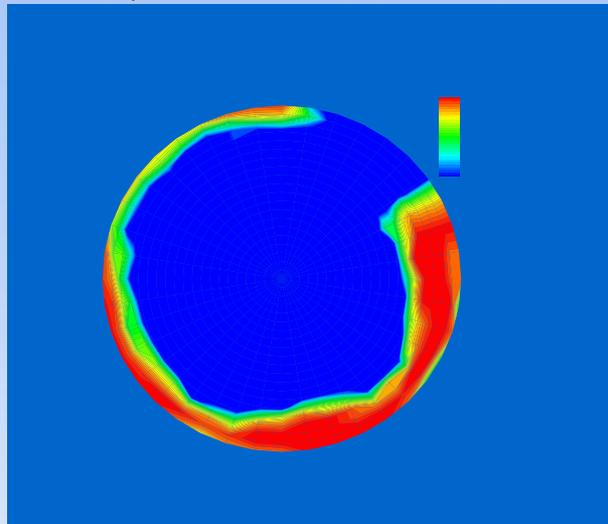
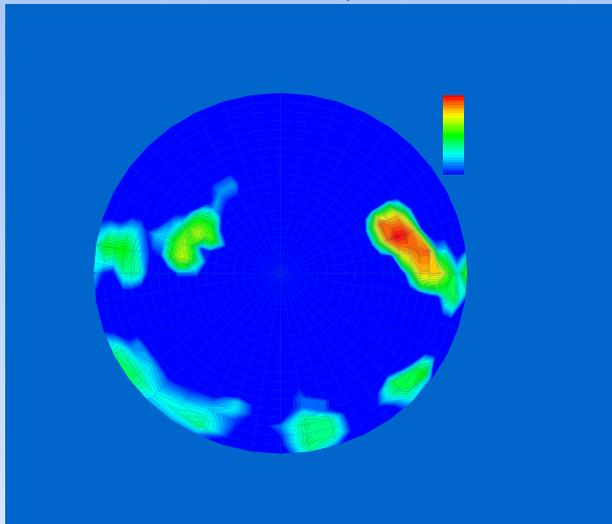
Vertical

Electrostatic field strength calculated for charged pipe wall (E: 1.22e5-1.22e7 V/m, 30 step)

# ECT & Electrostatic field

- particles at vertical pipe

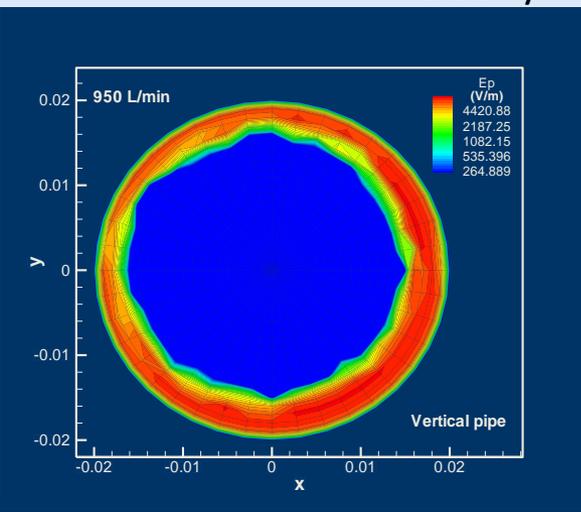
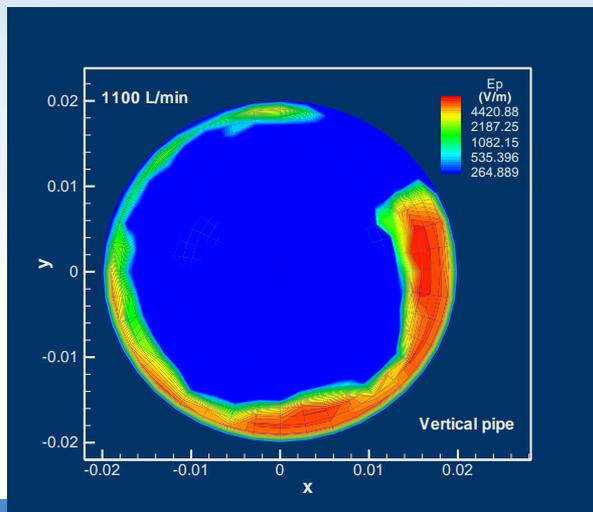
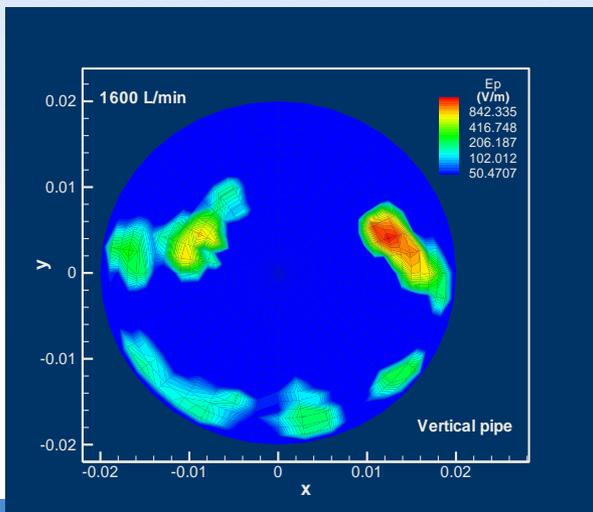
ECT solid fraction (Rao et al. 2001; Zhu et al. 2003)

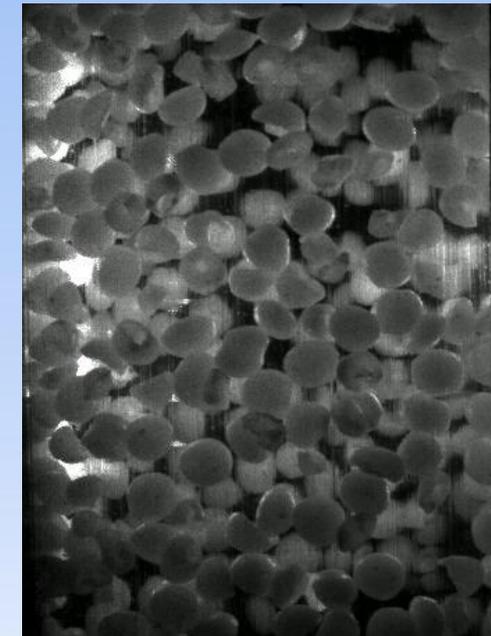
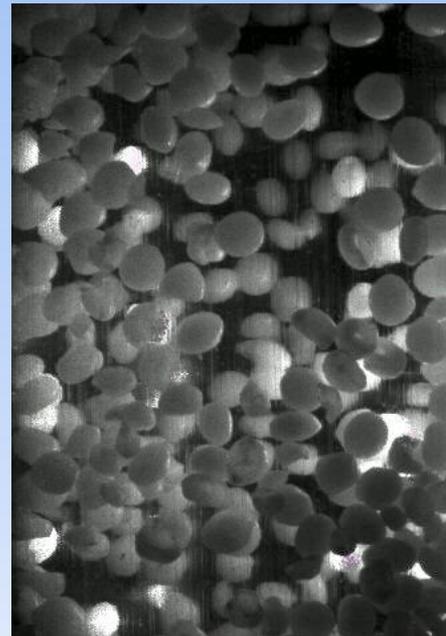


Electrostatic field 1600

1100

960 L/min






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Air flow rate (L/min)	1600 (left)	1100(middle)	950(right)
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(m/s):

Core region ( $r/R < 0.7$ ):

5.10

-

-

Boundary region ( $0.8 < r/R < 1.0$ ):

3.60

0.23

0.04

$F_D$  (N):

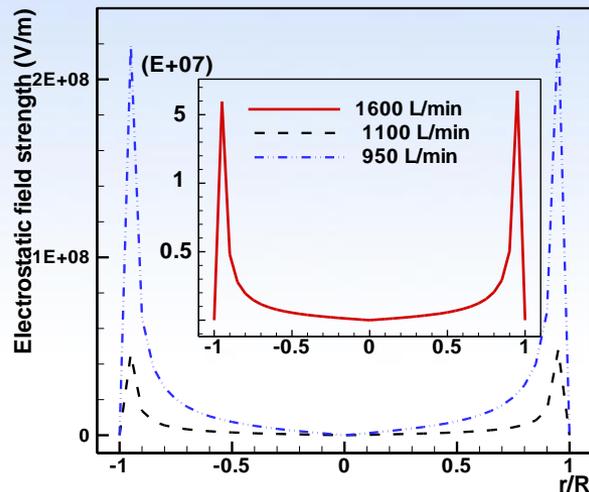
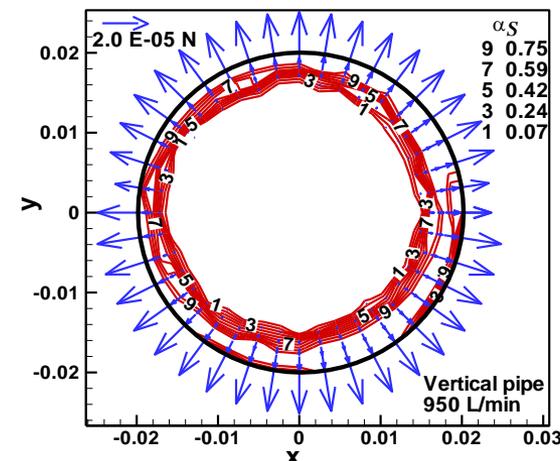
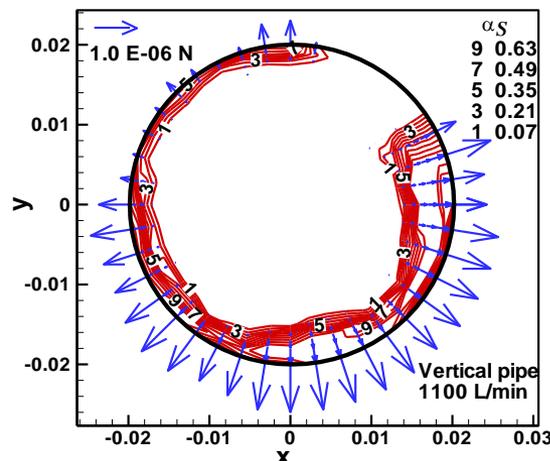
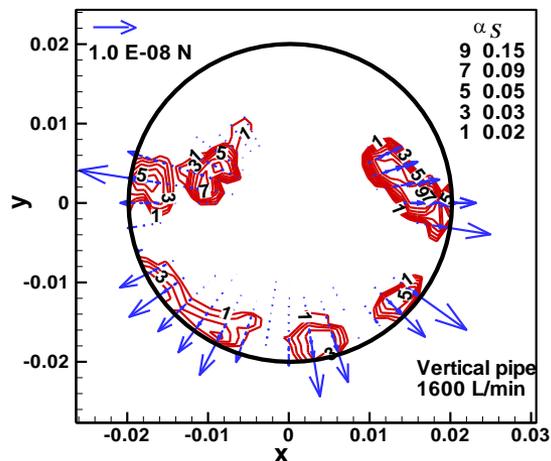
Boundary region ( $0.8 < r/R < 1.0$ ):

1.62E-02

9.89E-04

1.65E-04

# Electrostatic force - particles at vertical pipe



The highest electrostatic force appears near the pipe wall and degrades from the pipe wall to the pipe center.

Electrostatic force increases with decreasing air flow rate.

# Dynamics analysis - particles at vertical pipe

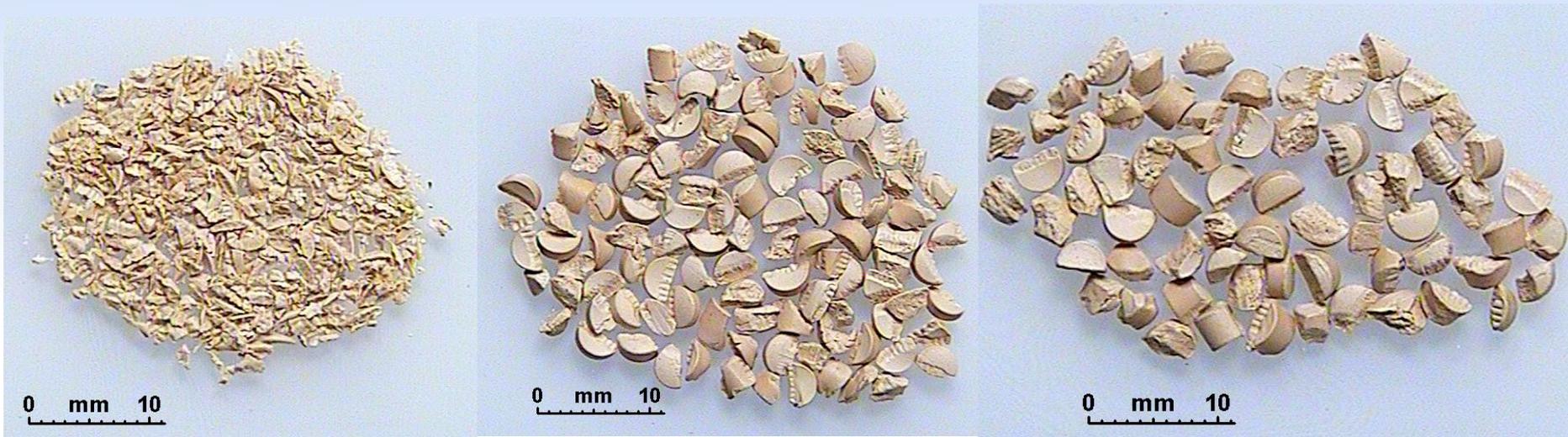
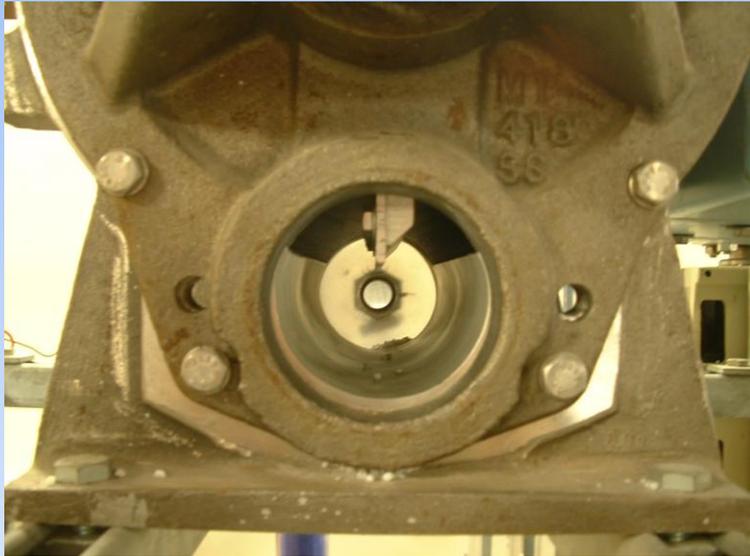
	Air flow rate (L/min)	Gravity (N)	$F_D$ (N)	$F_f$ (N)	$F_E$ (N)
Core region:	1600	1.27E-04	7.56E-02	2.62E-12~1.19E-09	4.68E-12~2.13E-09
Boundary region:	1600	1.27E-04	1.62E-02	1.00E-09~1.25E-08	1.79E-09~2.23E-08
	1100	1.27E-04	9.89E-04	5.26E-09~2.35E-06	9.39E-09~4.19E-06
	950	1.27E-04	1.65E-04	3.60E-07~1.89E-05	6.42E-07~3.37E-05

Core region:  $r/R < 0.7$ ; boundary region:  $0.8 < r/R < 1$ .

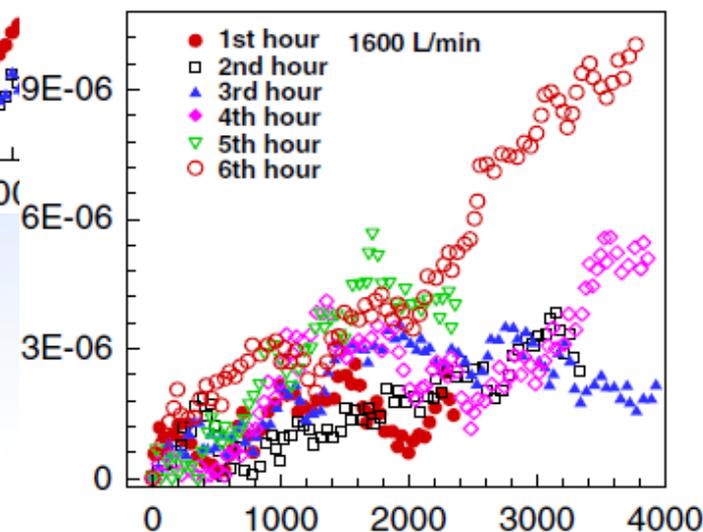
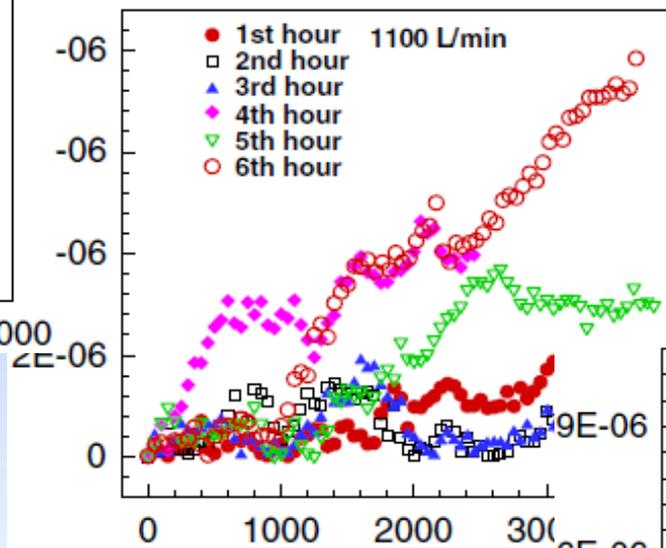
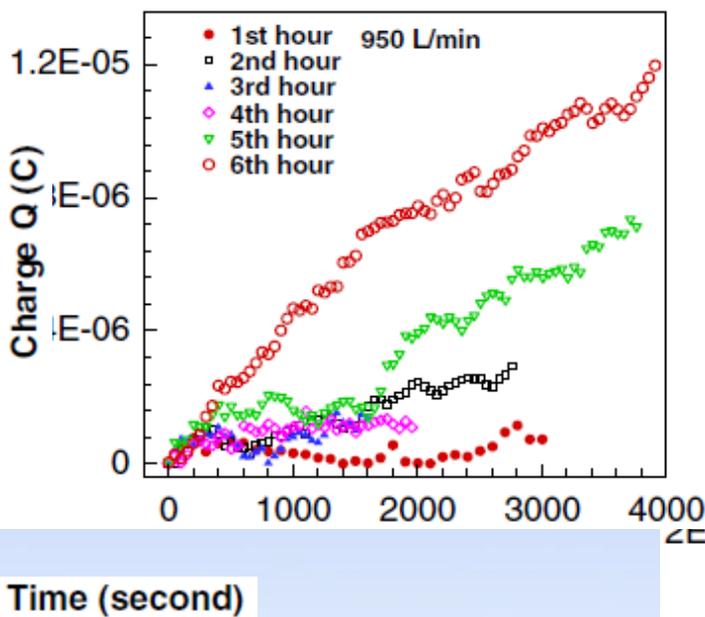
Lower air flow rates give rise to half-ring and ring flows. Fluid drag forces within the wall boundary layer are reduced to the same order of magnitude as that of gravitational forces. A dynamic equilibrium may be established between the two types of forces.

Electrostatic force may then emerge as the dominant factor affecting granule behavior.

# Granular attrition effect

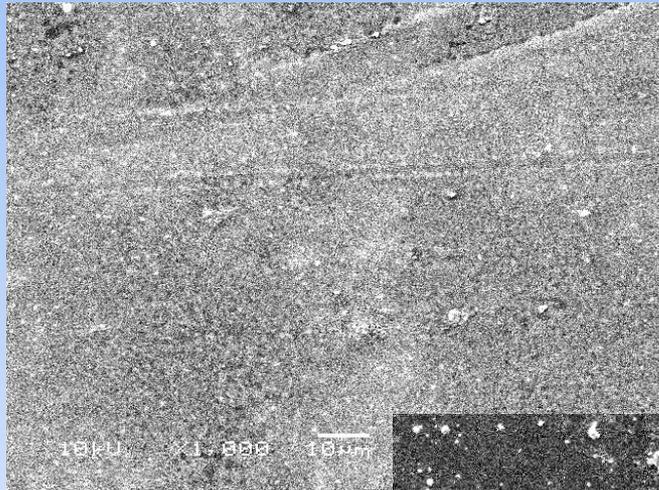


# Granular electrostatics – attrition

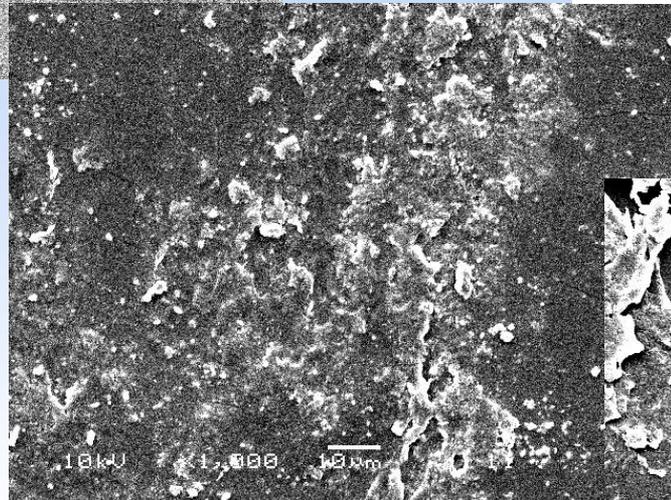
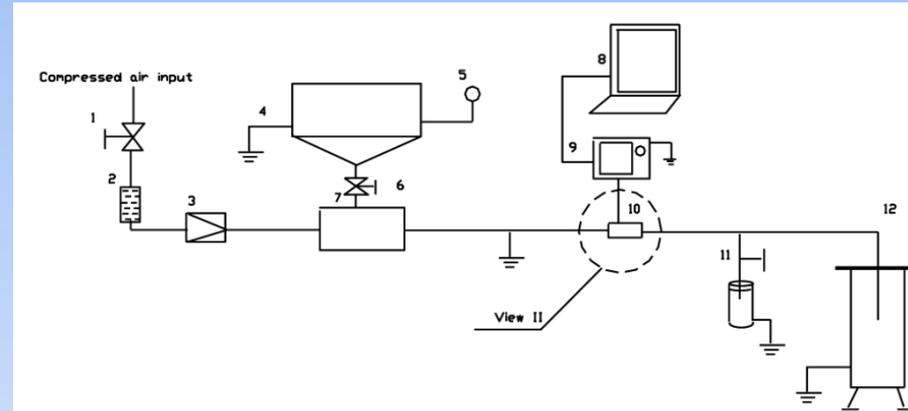


# Charge generation mechanism

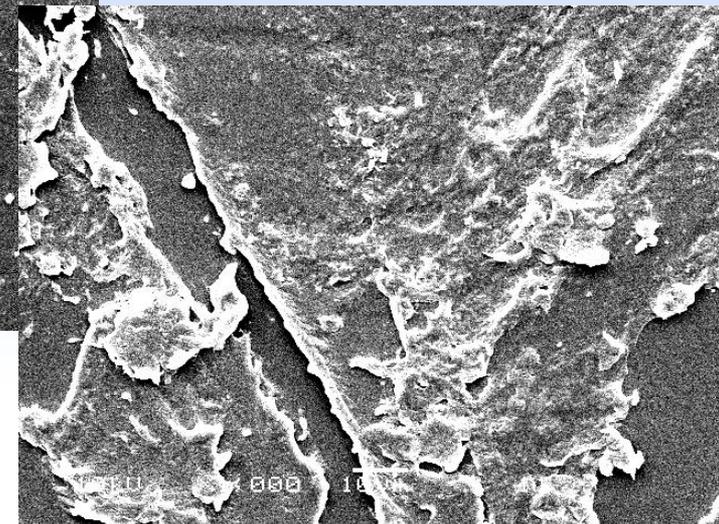
## - triboelectrification



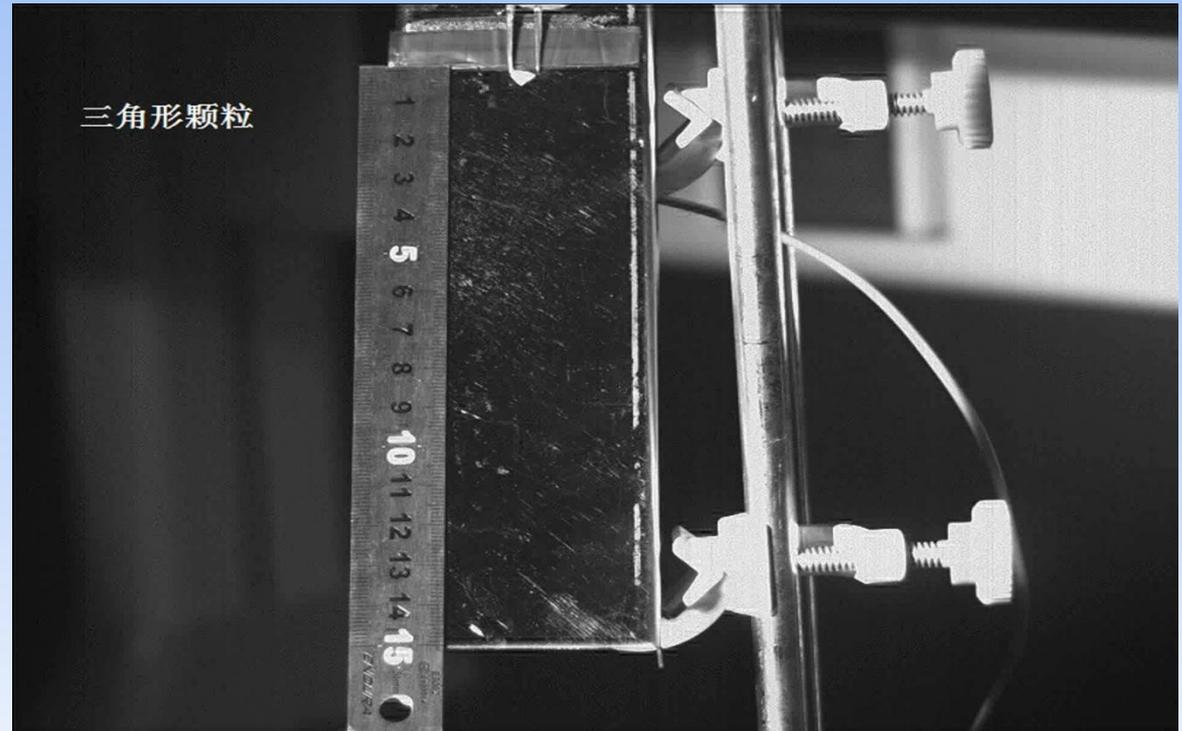
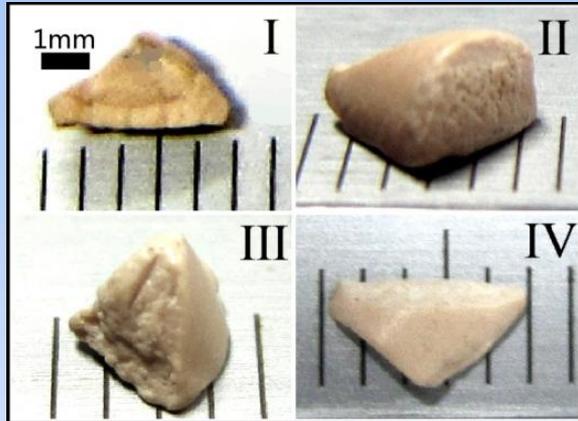
Fresh film



Used for 2 mins



Used for 10 mins



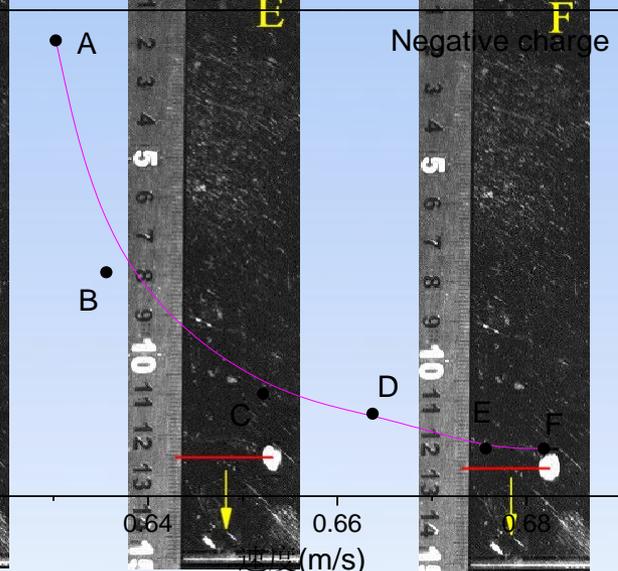
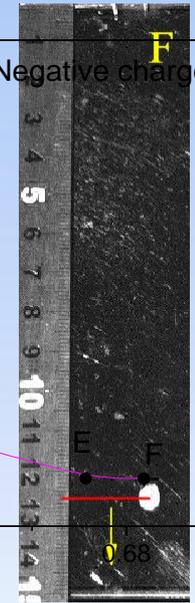
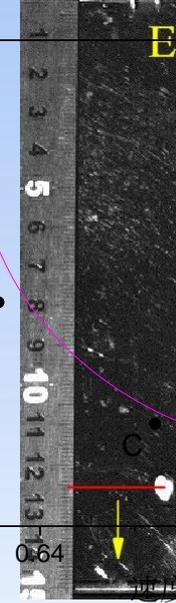
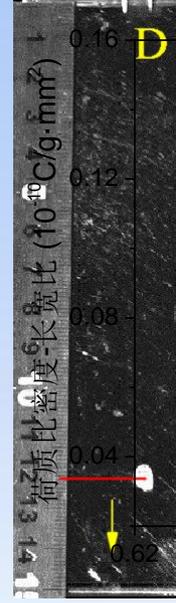
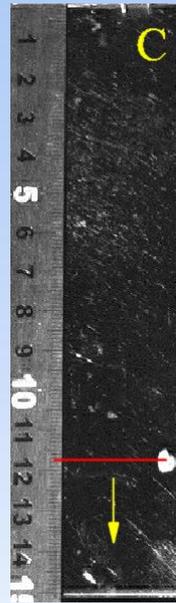
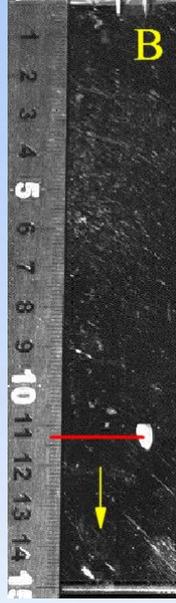
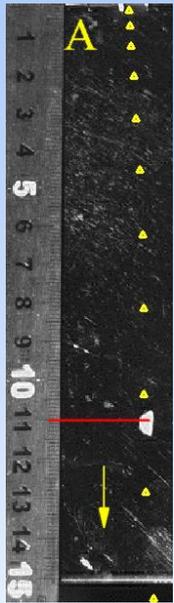
**Setup:** Faraday cage (TR8031, Advantest Corporation, Japan)

Electrometer (Advantest R8252 Digital Electrometer, Advantest Corporation, Japan)

High-speed camera (Japan: OLYMPUS, i-speed LT)

Stainless steel : 15cm\*5cm

$T = 0.2s$



Electrostatics at corresponding point

Time cost:

0.238s

0.236s

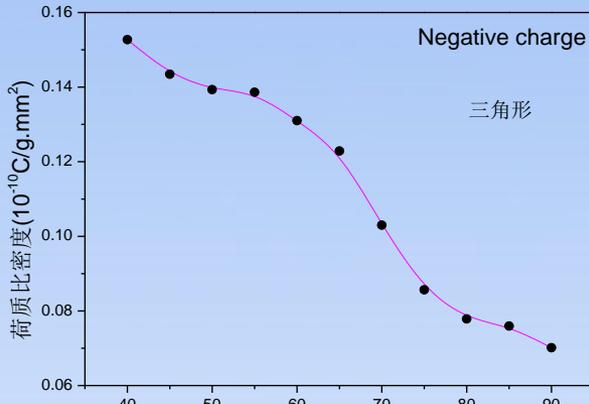
0.230s

0.226s

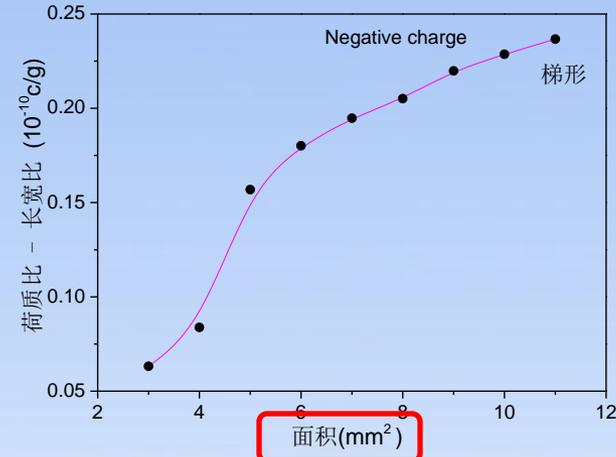
0.222s

0.220s

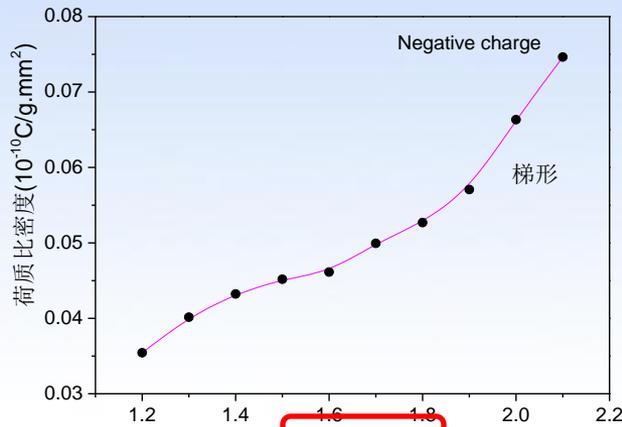
# Granular shape effect



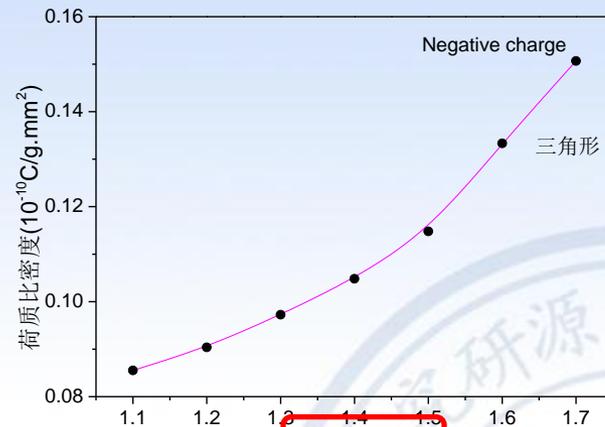
Front-facing angle



Area



Length ratio



Length ratio

- In the granular conveying system, air flow rate is a key factor determining the electrostatic behavior of granular flow. The lower the air flow rate, the higher the induced current and particle charge density. These in turn lead to particle clustering and the formation of such structures as half-ring and ring in the vertical conveying pipe.
- The electrostatics of granular flow in a pneumatic conveying system was quantitatively characterised by induced current, particle charge density and equivalent current of the charged granular flow and found to increase with granular attrition occurring in the rotary valve. A new method using granule size and shape is proposed as a useful tool for characterisation of electrostatics in general systems where granules are made up of complex combinations of different sizes and geometries.
- Granular size/shape due to attrition is found to affect electrostatic charge generation characteristics. It was found that some factors, such as granular front-facing angle, length-ratio, sliding direction, sliding times and environmental relative humidity, had significant effects on granular electrostatics generation.
- The mechanism of electrostatic charge generation for the granular flow in the pneumatic conveying system mainly depends on triboelectrification due to strong force effect on the surface when the particles slide on the pipe wall.

## Acknowledgements

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